Saction	1. Ra	lancod	Troos	Solutions	
section	4. Da	ianceo	rrees	Solutions	5

0. The ABC's of AVL	Trees
---------------------	-------

		ne	AL		5 ()I A	VL	116	ees						
									-					When shMap?	
1.	L	.et'	s P	lar	nt a	ın A	\V L	. Tr	ee						
ns	ert	10,	4,	5, 8	3 , 9	, 6,	11,	3,	2, 1	, 14 ir	nto an i	nitially	/ empt	y AVL 7	Ггее.

2. MinVL Trees

aw an AVL	tree of heig	ht 4 that co	ontains the	minimum p	ossible nu	ımber of noo	les.
							_
AVL		1 10	^ 0 7	into an initi	ally omnty	· ^\/I Troo	
seri 6, 5,	4, 3, 2,	⊥, ⊥∪, 	9, 8, 1	Into an niio	ally empty	AVL IIEE.	

4. The ABC's of B-Trees

	What properties must a B-tree of n values have with given values for M and L?
b)	Give an example of a situation that would be a good job for a B-tree. Furthermore, are there any constraints on the data that B-trees can store?
b)	

5. Implement a B-Tree? Nah, Let's Analyze!

Given the following parameters for a B-Tree with a page size of 256 bytes:

- Key Size = 8 bytes
- Pointer Size = 2 bytes
- Data Size = 14 bytes per record (includes the key)

Assuming that M and L were chosen appropriately, what are M and L? Recall that M is defined as the maximum number of pointers in an internal node, and L is defined as the maximum number of values in a leaf node. Give a numeric answer and a short justification based on two equations using the parameter values above.

,	, '	stor varaco e	

6. Oh, B-Trees

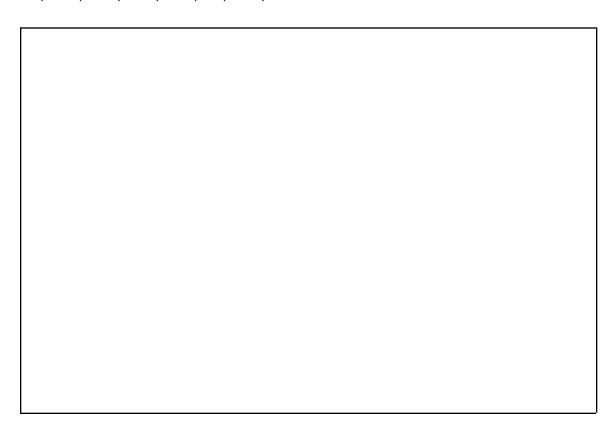
Find a tight upper bound on the worst case runtime of these operations on a B-tree. Your answers should be in terms of M, L, and n.

a)	Looking up the value of a key
b)	Inserting and deleting a key-value pair

7. B-Trees

a)	Insert the following	into an	empty B-Tree	with $M =$	3 and L = 3:
----	----------------------	---------	--------------	------------	----------------

12, 24, 36, 17, 18, 5, 22, 20



b) Delete 17, 12, 22, 5, 36



c)	Given the following parameters for a B-Tree with $M=11$ and $L=8$ - Key Size = 10 bytes
	Pointer Size = 2 bytesData Size = 16 bytes per record (includes the key)
	- Data Size - 10 bytes per record (includes the key)
	Assuming that M and L were chosen appropriately, what is the likely page size on the machine where this implementation will be deployed? Give a numeric answer and a short justification based on two equations using the parameter values above.

8. It's Fun to B-Trees!

a) Insert the following into an empty B-Tree with M=3 and L=3: 3, 32, 9, 26, 6, 21, 8, 4, 5, 30, 31 b) Delete 4, 5, 21, 9, 31, 3, 26, 8